

Chapter 2

$$(1) \langle v(t) \rangle = \frac{1}{T_0} \int_{T_0} v(t) dt; (2) p \triangleq \langle |v(t)|^2 \rangle = \frac{1}{T} \int_{T_0} |v(t)|^2 dt; (3) \langle v(t-t_0) \rangle = \frac{1}{T} \int_{T_0} |v(t)|^2 dt, C_n = \frac{1}{T_0} \int_{T_0} v(t) e^{-j2\pi n f t} dt$$

$$(4) \frac{A\tau}{T_0} \sin c(\tau n f_0); (5) A \tau \text{sinc}(f \tau) = F[\pi(t/\tau)]; (6) A \tau \text{sinc}^2(f \tau) = F[\Lambda(t/\tau)]; (7) \begin{cases} z(t) = V(t) \\ F[z(t)] = v(-f) = Z(f) \end{cases};$$

Chapter 3

$$(1) E_y = \int_{-\infty}^{+\infty} |H(f)|^2 |X(f)|^2 df; (2) |H(f)| = |k| \arg H(f) = -2\pi t_d f; (3) H_{eq}(f) = \frac{k e^{-j\omega t_d}}{H(c)}$$

$$(4) H_{eq}(f) = \left(\sum_{m=-M}^M c_m e^{j\omega_m \Delta} \right) e^{-j\omega_m \Delta}; (5) g \triangleq P_{out}/P_{in}, P_{out_{dbm}} = g_{db} + P_{in_{dbm}}, P_{dbm} = 10 \log \frac{P}{1mW}$$

$$(6) L \triangleq \frac{1}{g} \frac{P_{in}}{P_{out}}, P_{out_{db}} = P_{in_{db}} - L_{db}; (7) P_{out} = 10^{-(\alpha L/10)} P_{in} \quad L_{db} = \alpha L;$$

$$(8) BPF: H(f) = \begin{cases} k e^{-j\omega t_d} & f_L \leq |f| \leq f_U \\ 0 & \text{otherwise} \end{cases}; (9) LPF: H(f) = k e^{-j\omega t_d} \prod \left(\frac{f}{2B} \right); (10) Bateworth: H(f) = \frac{1}{\sqrt{1+(f/B)^{2n}}}$$

$$(11) H_Q(f) = -j \text{sgn}(f) = \begin{cases} -j & f > 0 \\ +j & f < 0 \end{cases}; (12) F\{\hat{x}(t)\} = (-j \text{sgn} f) X(f); (13) \langle v(t) w^*(t) \rangle^2 \leq P_v P_w$$

$$(14) R_{vw}(\tau) \triangleq \langle v(t) w^*(t-\tau) \rangle = \langle v(t+\tau) w^*(t) \rangle; (15) |R_{vw}(\tau)|^2 \leq P_v P_w, R_{vw}(\tau) = R_{vw}^*(-\tau), R_v(0) = P_v, |R_v(\tau)| \leq R_v(0)$$

$$(16) v(t) = c_v e^{j\omega_v t}, w(t) = c_w e^{j\omega_w t}, R_{vw}(t) = \begin{cases} 0 & \omega_v \neq \omega_w \\ c_v c_w^* e^{j\omega_v t} & \omega_v = \omega_w \end{cases}; (17) R_{vw}(\tau) \triangleq \int_{-\infty}^{+\infty} v(t) w^*(t-\tau) dt, R_v(\tau) \triangleq R_{vv}(\tau), |R_{vw}(\tau)|^2 \leq E_v E_w;$$

$$(18) \int_{-\infty}^{+\infty} G_v(f) df = R_v(0), G_v(f) = |H(f)|^2 G_x(f), R_v(\tau) \leftrightarrow G_v(f)$$

Chapter 4

$$(1) v_{bp}(t) = A(t) \cos[\omega_c t + \phi(t)]; (2) v_i \triangleq A(t) \cos \phi(t), v_q \triangleq A(t) \sin \phi(t), A(t) = \sqrt{v_i^2(t) + v_q^2(t)}, \phi(t) = t g^{-1} \frac{v_q(t)}{v_i(t)};$$

$$(3) v_{ip}(t) = \frac{1}{2} A(t) e^{j\phi(t)}, v_{bp}(t) = 2 \text{Re}\{v_{ip}(t) e^{j\omega_c t}\}; (4) A_m: A(t) = A_c [1 + \mu x(t)], x_c(t) = A_c [1 + \mu x(t)] \cos \omega_c t;$$

$$(5) S_T = \frac{1}{2} A_c^2 (1 + \mu^2 S_x); (6) DSB: x_c(t) = A_c x(t) = A_c x(t) \cos \omega_c t, s_T = \frac{1}{2} A_c^2 S_x;$$

$$(7) SSB: x_c(t) = \frac{1}{2} A_c A_m \cos(\omega_c \pm \omega_m) t, x_{LP}(t) = \frac{1}{2} A_c x(t), A(t) = \frac{1}{2} A_c \sqrt{x^2(t) + \hat{x}^2(t)}, x_c(t) = \frac{1}{2} A_c [x(t) \cos \omega_c t \mp \hat{x}(t) \sin \omega_c t];$$

Chapter 5

$$(1) FM \& PM: x_c(t) = A_c \cos(\omega_c t + \phi(t)); (2) \theta_c(t) = \omega_c t + \phi(t) \& \frac{1}{2\pi} \theta = f(t); (3) x_c(f) = \frac{1}{2} A_c \delta(f - f_c) + \frac{j}{2} A_c \Phi(f - f_c) \quad F > 0;$$

$$(4) FM: \phi(t) = 2\pi f_\Delta \int_0^t x(\lambda) d\lambda, f(t) = f_c + f_\Delta x(t); PM: \phi(t) = \phi_\Delta x(t), f(t) = \frac{1}{2\pi} \phi_\Delta \dot{x}(t) + f_c; (5) \begin{cases} \phi(t) = \beta \sin \omega_m t \\ \beta = \begin{cases} \phi_\Delta A_m & PM \\ (A_m/f_m) f_\Delta & FM \end{cases} \end{cases}$$

$$(6) x_c(t) = A_c \sum_{n=-\infty}^{+\infty} J_n(\beta) \cos(\omega_c + n \omega_m) t; (7) \beta = 2M(\beta) f_m \text{ when } M(\beta) \gg 1;$$

$$(8) FM: B_T = 2(D+1)W, \text{ for } D \gg 1 \& D \ll 1, D = \frac{f_\Delta}{W}, \quad PM: B_T = 2(\phi_\Delta + 1)W;$$

Chapter 6

$$(1) x_\delta(t) = x(t) \delta(t) \quad f_s > 2w; (2) S_\delta(t) = \sum_{k=-\infty}^{+\infty} \delta(t - kT_s); (3) x_\delta(t) \triangleq x(t) S_\delta(t);$$

$$(4) S_\delta(f) = F_s \sum_{n=-\infty}^{+\infty} \delta(f - n f_s); (5) x_p(t) = \sum_k x(kT_s) P(t - kT_s); (6) X_p(f) = p(f) \left[f_s \sum_n x(f - n f_s) \right] = p(f) x_\delta(f);$$

$$(7) PDM: \tau_k = \tau_0 [1 + \mu x(kT_s)] \quad PPM: t_k = kT_s + t_d + t_0(kT_s); (8) B_T \gg \frac{1}{2T_r}; (9) PAM: A_0 [1 + \mu x(t)]$$